

# Strategic Capacity Investments under Hold-up Threats

## The Role of Contract Length and Width

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# Commodities and equipment

- Many commodities can be consumed only with some specific equipment: e.g. for heating, fuel + heater.
- Once equipped with an appliance, a consumer is trapped with the corresponding commodity  
→ short-run elasticity is low, and the seller of the commodity can exert market power.
- But in the long run, appliances can be replaced: the commodity seller should not abuse his market power.  
On the contrary, he should encourage consumer equipment. How?
- He may announce a reasonable commodity price to encourage investment, but is he credible?  
If commitment is limited (short contract), buyers may fear *hold-up*.

Is a longer contract the best way to encourage investment?

# Commodities and equipment: demand

Bilateral relationship with a purely relationship-specific investment.

- First, the buyer invests in an equipment with capacity  $A$ .
- Then he can consume less than  $A$ , but not more.  
Example: natural gas imports cannot exceed the pipeline capacity.

Once  $A$  is fixed, demand is both elastic and rigid:

- Consumption has a price elasticity  $\varepsilon$  as long as it does not exceed the investment capacity  $A$ : inverse demand function  $P(q)$ .
- Then it is completely inelastic:  $q = A$ .

# Contracts

- Before the buyer invests, the seller offers him a contract characterized by
  - A pricing scheme (two-part tariff / linear prices).
  - A duration ( $T$ , from 0 to  $\infty$ ).
- Contracts with limited “width” may be optimized with respect to length in compensation.
- In the absence of uncertainty, is the longest contract always the best?
- Who pushes for longer contracts? Do the parties agree on an optimal duration?

# References

- Commodities and appliances: econometric literature on estimation of consumer demand:  
Dubin-McFadden (1984), Hanemann (1984), Balestra and Nerlove (1966).
- Standard competition or after-market monopolisation:  
Shapiro (1995), Chen *et al.* (1998), Reitzes and Woroch (2008).
- Contract length and width:  
Crocker and Masten (1988), Joskow (1988).

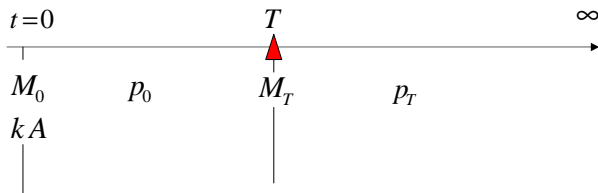
# General setting: Contracts (1)

## Timing

- 1 The seller offers a contract valid from  $t = 0$  to  $T$ : fixed fee+unit fee  $(M_0, p_0)$ .
- 2 The contract is accepted or not. Game continues if accepted.
- 3 The buyer invests  $A$  (unit cost  $k$ ) before trade begin.
- 4 The quantity  $q_0$  is chosen freely by the buyer at each moment (it cannot be specified in the contract). The seller produces at cost  $c$ .
- 5 At  $T$  the contract expires, the seller sets a new pricing scheme  $(M_T, p_T)$ . The buyer consumes  $q_T$  at each moment indefinitely.

The discount rate is  $r$ .

## General setting: Contracts (2)



- 1st stage ( $t = 0$  to  $T$ ): at the moment the contract is signed, the investment level can still be adjusted.
- 2nd stage ( $t = T$  to  $\infty$ ): at expiry of the contract, the investment cost is sunk: hold-up risk.

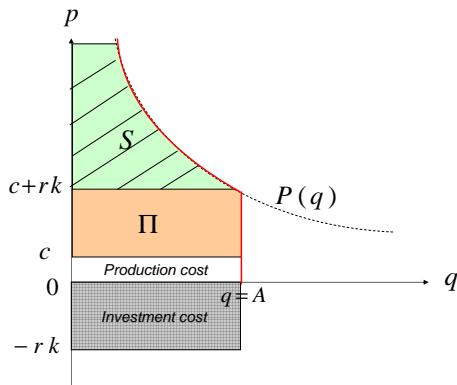
# Social optimum

Social surplus:

$$W = \int_0^{\infty} e^{-rt} [U(q_t) - cq_t] dt - kA = \frac{1}{r} (S_t + \Pi_t - rkA)$$

- Let  $P = U'$  and  $Q = P^{-1}$ .
- At social optimum

$$q = A = Q(c + rk).$$





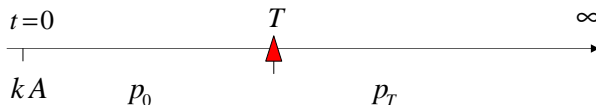
# Nonlinear tariffs

- When  $T = \infty$ , the social optimum can be attained:  $p_0 = c$  gives the buyer the right incentive to invest  $A = Q(c + rk)$ , and  $M_0$  allows the seller to capture all the surplus.
- When commitment is limited, the buyer anticipates hold-up after contract expiry (after  $T$ ). But the seller can set  $p_0 < c$  (consumption subsidy) to give the right investment incentives, and increase  $M_0$  to get all the first-stage surplus. Then from  $T$  on, the seller can again capture the entire second-stage surplus.
- When the seller cannot commit ( $T = 0$ ), the optimum cannot be attained: once  $A$  is invested, the seller will set a "hold-up" price. Knowing this, the buyer will **not** invest.

# Nonlinear tariffs: surplus sharing

- Whenever some seller commitment is possible, the seller can achieve the socially optimal investment with two-part tariffs. But the buyer gets no surplus.
- Linear tariffs are less efficient, but they always leave the buyer with some surplus.  
→ they may be imposed in the buyer's interest to protect him against full rent extraction.

# Linear tariffs



The contract seems to protect the investor from hold-up. The longer, the better?

## Contract-Investment Paradox

The investment level **decreases** with respect to the contract duration.

# Effects

- $p_T$ : **Classical hold-up effect.** When the buyer invests, he incurs costs that maybe he will not recover due to hold-up from  $T$  on. This investment-**detering** effect decreases as  $T$  increases.
- $A$ : **Hold-up mitigating effect.** By investing, the buyer "commits" to a higher demand, which allows him to obtain lower prices after contract expiry, from  $T$  on. This investment-**enhancing** effect decreases as  $T$  increases.
- $p_0$ : **Contract leverage effect.** The seller can use the contract price as a tool to stimulate investment (set a low  $p_0$ , valid until  $T$ ). In case he does, this investment-**enhancing** effect increases as  $T$  increases.

# Active/Passive

## Definition

The **buyer** is *active* when his investment choice  $A$  induces a response  $p_T$  from the seller that differs from the unconstrained monopoly price  $\frac{\varepsilon c}{\varepsilon - 1}$ . Otherwise he is *passive*.

## Definition

The **seller** is *active* when his price choice  $p_0$  induces a response  $A$  from the buyer that differs from  $A = Q(p_0)$ . Otherwise he is *passive*.

## Theorem (Equilibrium prices in the general case)

- 1 If  $\frac{c}{rk} \geq (\varepsilon - 1)e^{rT}$ , both parties are passive and

$$p_0 = p_T = \frac{\varepsilon c}{\varepsilon - 1}.$$

- 2 If  $(\varepsilon - 1)e^{rT} - \frac{1}{\varepsilon} \leq \frac{c}{rk} < (\varepsilon - 1)e^{rT}$ , the buyer is active and the seller is passive, and

$$p_0 = p_T = re^{rT} \varepsilon k.$$

- 3 If  $\frac{c}{rk} < (\varepsilon - 1)e^{rT} - \frac{1}{\varepsilon}$ , both parties are active and

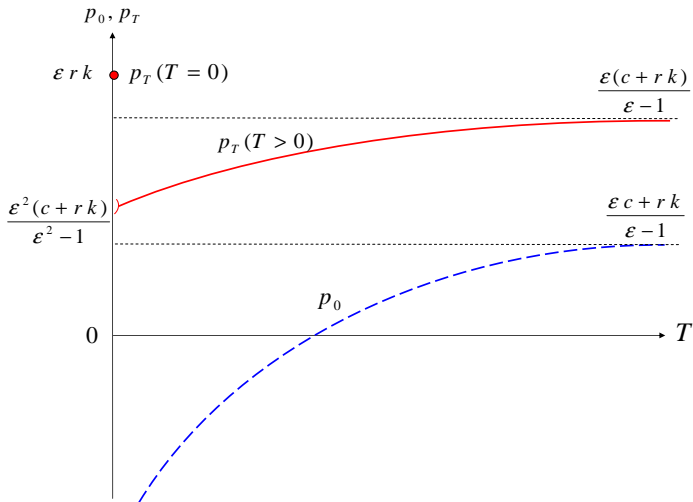
$$\begin{cases} p_0 &= \frac{1}{1 - e^{-rT}} \left[ \left( 1 - \frac{\varepsilon e^{-rT}}{\varepsilon + e^{-rT}} \right) \frac{\varepsilon c}{\varepsilon - 1} + \left( 1 - \frac{\varepsilon^2 e^{-rT}}{\varepsilon + e^{-rT}} \right) \frac{rk}{\varepsilon - 1} \right], \\ p_T &= \frac{\varepsilon^2 (c + rk)}{(\varepsilon + e^{-rT})(\varepsilon - 1)}. \end{cases}$$

# Active/Passive

When the investment cost is sufficiently high, both parties will be active whatever  $T$ . At equilibrium,

- $q_t = A$  for all  $t$ : capacity is never idle;
- $p_T = P(A) > \frac{\varepsilon c}{\varepsilon - 1}$ : active buyer, induces the seller to adjust  $p_T$  to capacity  $A$ ;
- $p_0 < p_T$ : active seller, subsidizes consumption to encourage investment.

# Equilibrium prices as a function of $T$





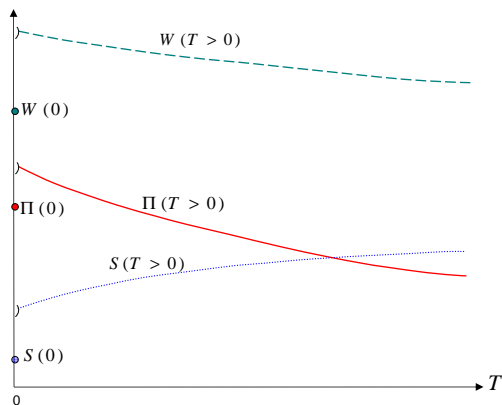
# Impact of contract duration on prices and investment

## "Bargain then Rip-off"

- Everybody knows the seller will exert hold-up from  $T$  on:  $p_T = P(A)$ .
- Since  $k$  is large, the buyer is not willing to invest much. The seller suffers from small volumes due to under-investment.
- The seller can use  $p_0$  as a tool to stimulate investment: offer a bargain until  $T$ .
- The smaller  $T$ , the better the bargain must be:  $p_0 \rightarrow -\infty$  when  $T \rightarrow 0$ .
- But when  $T = 0$ , no contract price  $p_0$ , no tool so stimulate investment: investment falls, the price jumps, and both profits and consumer's surplus fall.

To increase investment, the smallest contract is the best, no contract at all is the worst.

# Surpluses and welfare as a function of $T$



- The seller's profit decreases with  $T$ .
- The buyer's surplus increases (hold-up occurs later).

# Summary of results

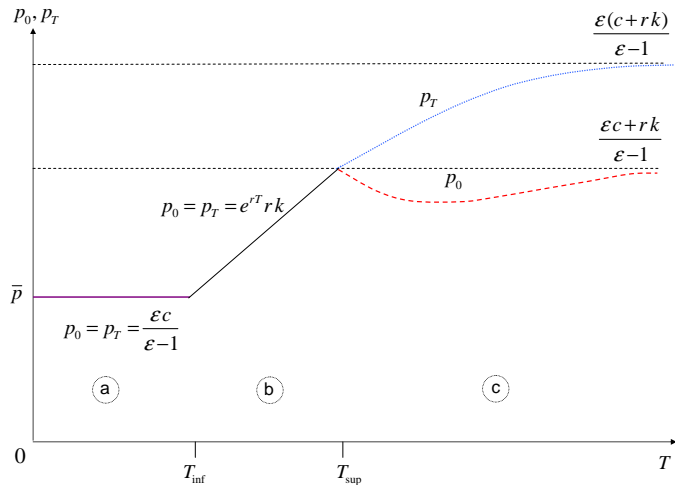
## Paradox

The longer the contract, the smaller the investment

- Therefore social welfare decreases with the contract duration, even though there is no need for flexibility (uncertainty).
- The seller always prefers a shorter contract.
- The buyer prefers the longest possible contract when the investment cost is high. When this cost is low, he can be better off with the shortest possible contract.
- If the investment cost is high, no contract is the worst solution, and a very short contract is the best for social welfare.

# Backup slides

# Impact of $T$ when $k$ is small: Equilibrium prices



# Impact of $T$ when $k$ is small: Intuitions (1)

Suppose the seller does not suffer too much from under-investment (no bargain with  $p_0$ :  $p_0$  is just chosen to have  $p_0 = P(A)$ ). For an intermediate  $T$ , what is the impact for the buyer of reducing  $A$ ?

- Immediate advantage: cost reduction ( $k$ )
- From  $T$  on, cost:  $p_T = P(A)$  will be higher.

## Zone ①: Low $T$

The "punishment" comes too soon, and since  $k$  is low the buyer prefers not to reduce  $A$  below  $Q(\frac{\varepsilon c}{\varepsilon - 1})$ .

Buyer accommodates, invests  $A = Q(\frac{\varepsilon c}{\varepsilon - 1})$ .

## Impact of $T$ when $k$ is small: Intuitions (2)

### Zone ⑥: Intermediate $T$

The punishment comes late enough, it is worth reducing  $A$ : Equalizing marginal cost/marginal benefit ( $k = \frac{e^{-rT}}{r} \frac{P(A)}{\varepsilon}$ ) yields  $A = Q(e^{rT} \varepsilon r k)$ .

But when  $T$  becomes large, the investment capacity decreases too much from the seller's point of view... He changes his strategy.

## Impact of $T$ when $k$ is small: Intuitions (3)

When  $A$  decreases too much, the seller stops setting  $p_0$  equal to the marginal willingness to pay of the buyer  $P(A)$ : he lowers  $p_0$  to stimulate investment. How low should be  $p_0$ ?

### Zone ©: Large $T$

- Immediate loss of revenues: lower price  $p_0 < P(A)$ .
- Profit increase from  $T$  on: higher volumes  $A$  at hold-up price  $p_T = P(A)$ .

⇒ good strategy as long as  $T$  is not too large.

When  $T \rightarrow \infty$  the profit increase is too remote: the seller increases  $p_0$  again, and  $p_0 \rightarrow p_{pA}$  for  $T \rightarrow \infty$ .